

Stochastic versus BFGS Training in Neural Discrimination of RF-Modulation

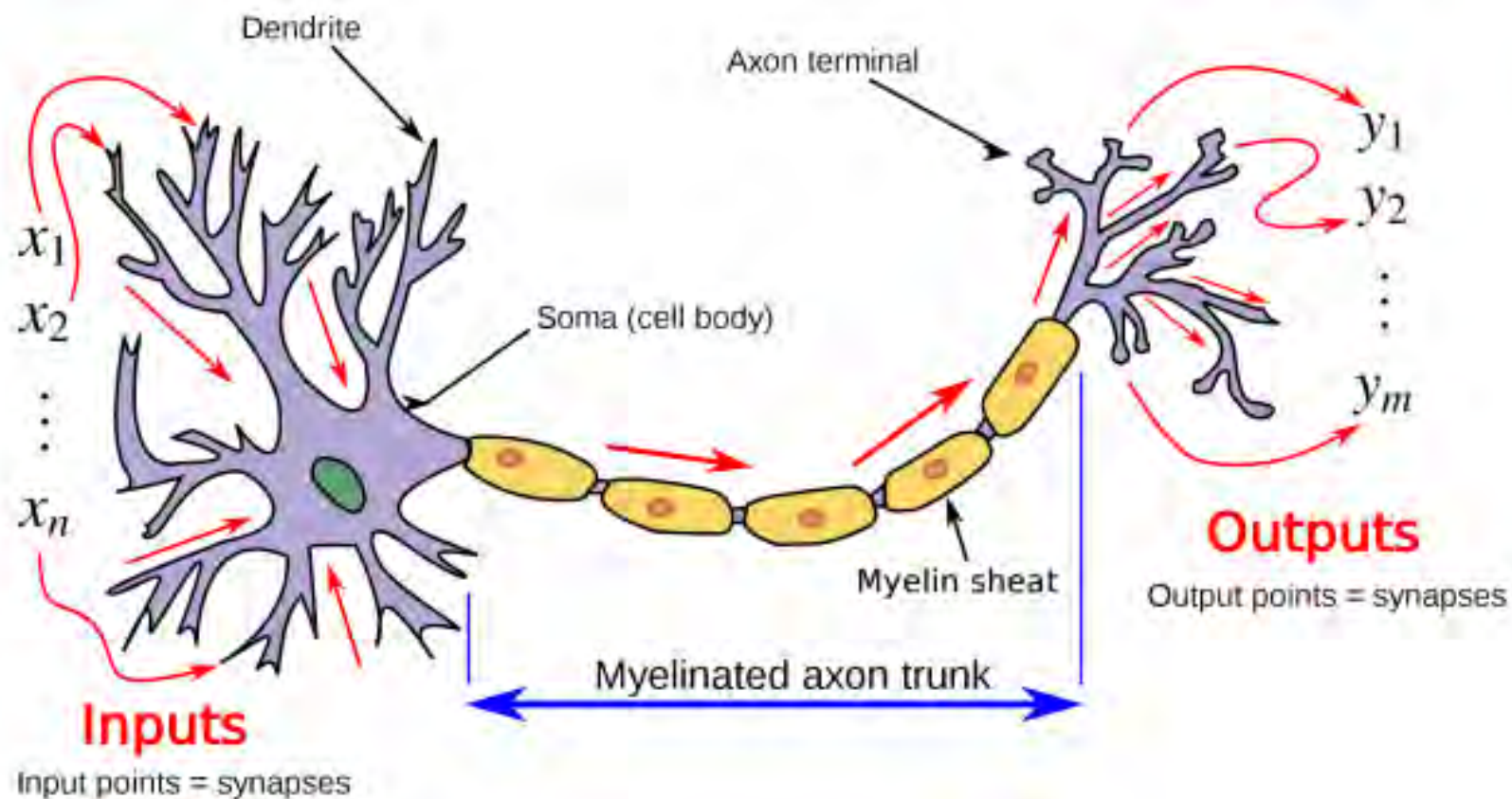
- 1 *Artificial intelligence*
- 2 *Wave reconstruction*
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- 4 *Results*
- 5 *Conclusions*

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Bio-analogy

- representation of data selection with:

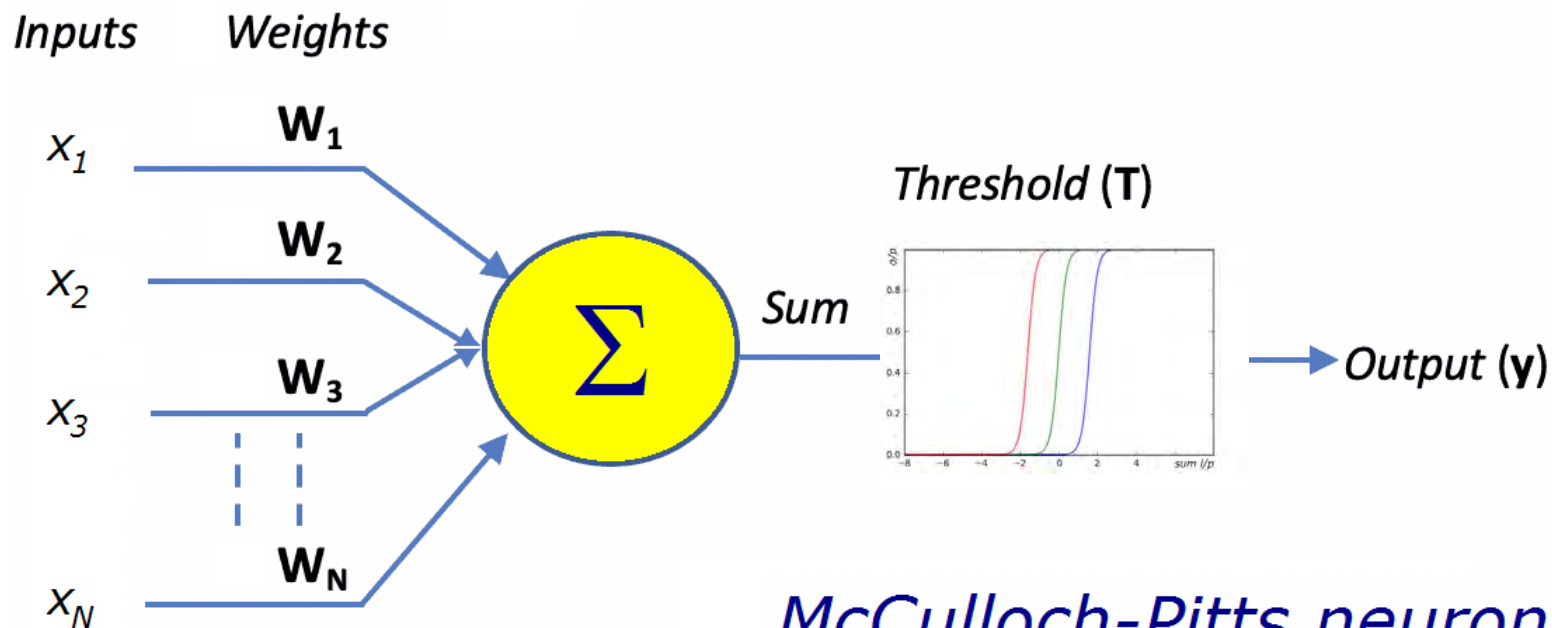
- **sum**
- **threshold**



Artificial Intelligence

- representation of data selection with:

- **sum**
- **threshold**



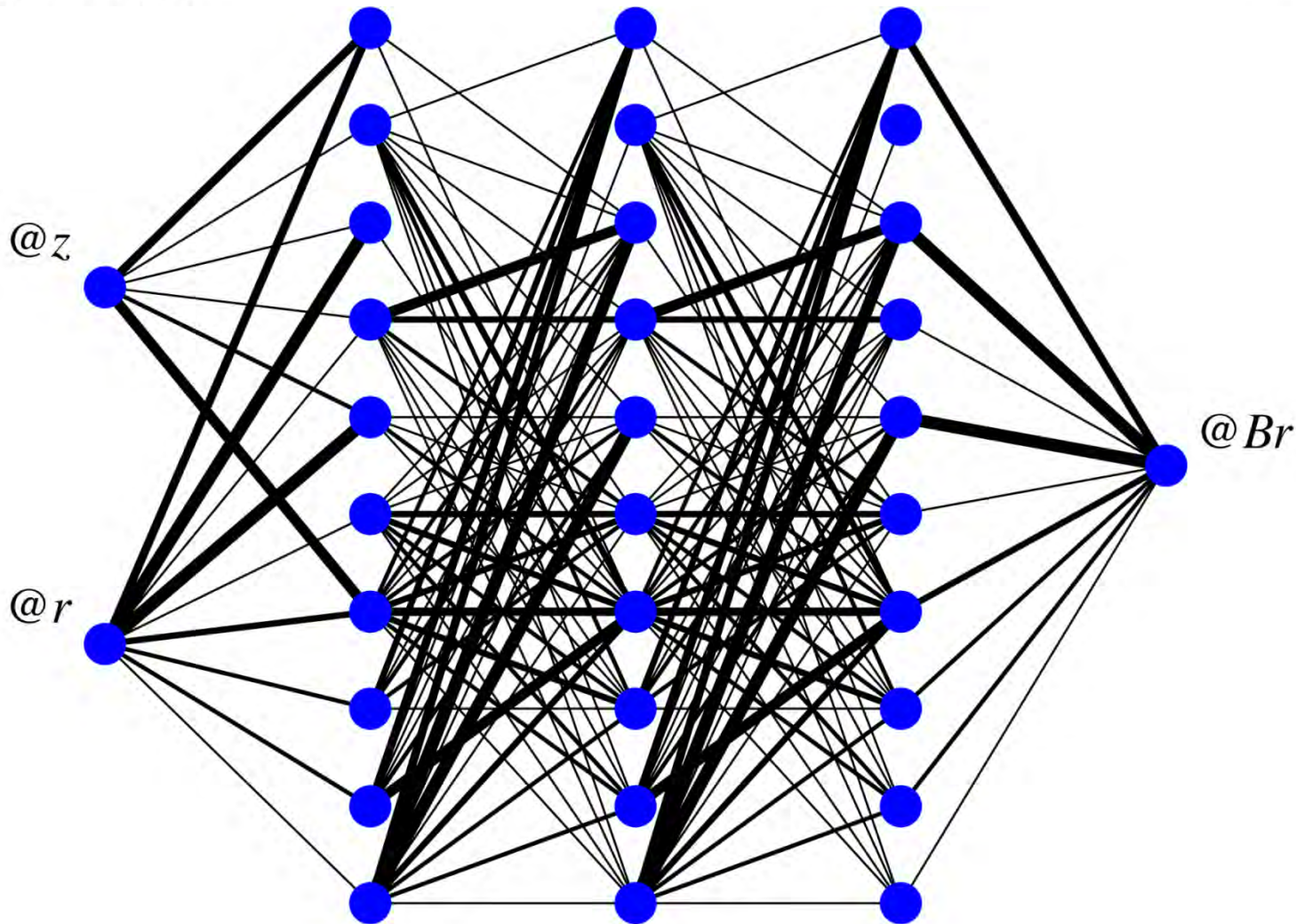
McCulloch-Pitts neuron

Multi-Layer Perceptrons @ ROOT

```
// show network structure
```

```
m1p->Draw()
```

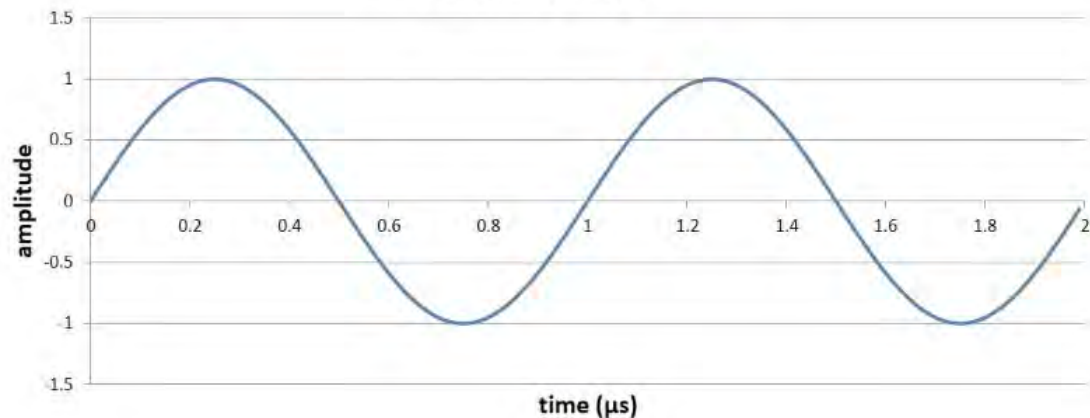
```
;
```



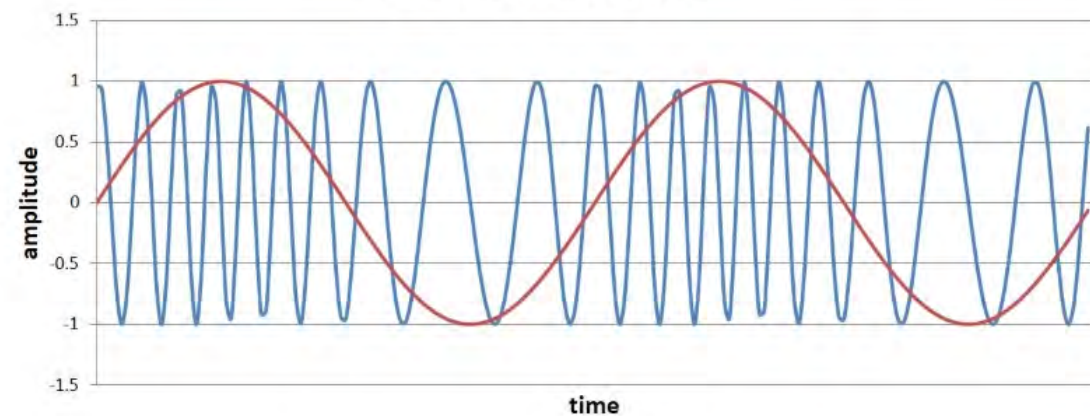
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Radio frequency modulation

Baseband Signal



Frequency Modulation



Shift keying:

- ASK, *amplitude*
- FSK, *frequency*
- PSK, *phase*
- ASK-LSB
- ASK-USB

Determination of: (*ped*, *A*, *f*, ϕ)

Magic sample number

- RF wave $y = p + A \sin(2\pi f t + \phi)$

sampling **1 : 3.675**

f_0 **12000 Hz**

Δ **1 / 44100 s**

- **pedestal**: find from average

$$\langle y \rangle = p + A_e \sin\left(2\pi f t \frac{t_i + t_f}{2} + \phi\right) \text{sinc}\left(\frac{2\pi f \Delta t}{2}\right)$$

$$A_e = \frac{A}{\text{sinc}(\pi f \Delta)}$$

- **magic N**: $\Delta t = 11\Delta \dots \delta p = 0.0023 A_e$

Amplitude

- same $N = 11$: $\langle \delta^2 y \rangle = A_e \langle \delta^2(\sin) \rangle$

Frequency

- same $N = 11$:
$$\begin{aligned} \langle y(y - y_{k\Delta}) \rangle &= pA_e(\langle \sin \rangle - \langle \sin_{k\Delta} \rangle) \\ &+ \\ &A_e^2(\langle \sin^2 \rangle - \langle \sin \cdot \sin_{k\Delta} \rangle) \\ &\simeq A_e^2 \sin^2\left(\frac{2\pi f k \Delta}{2}\right) \\ &\simeq \text{const} + \pi k \Delta A_e^2 \sin(2\pi f k \Delta) \cdot \delta f \end{aligned}$$

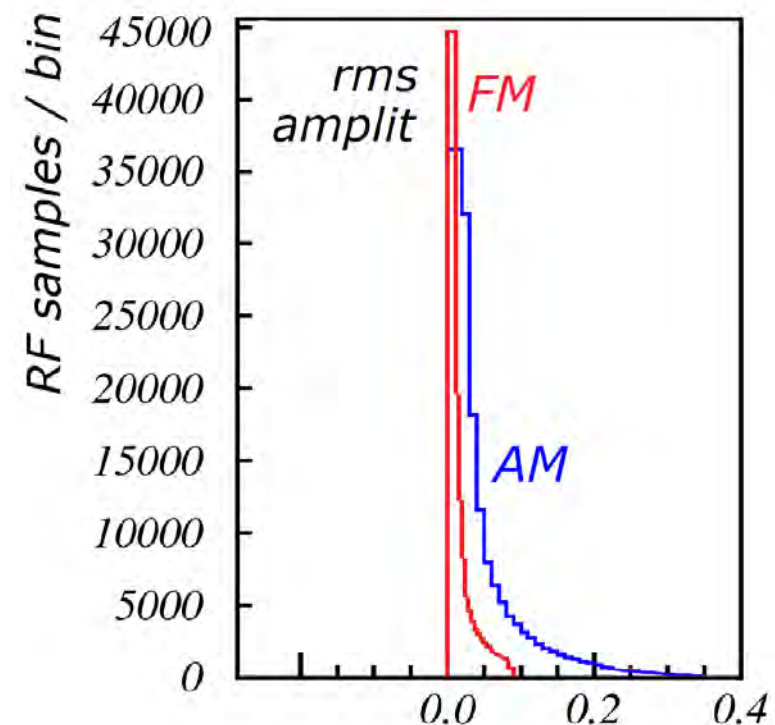
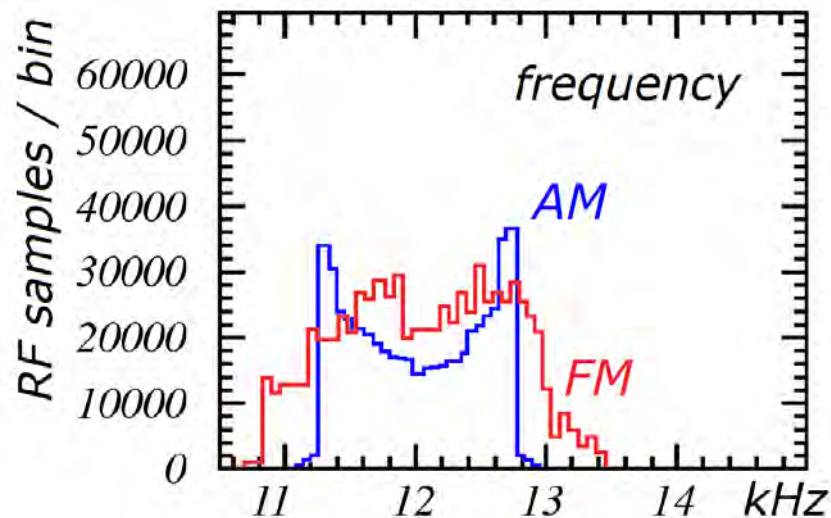
($k = 1$; max sensitivity)

Determination of: (*ped*, *A*, *f*, ϕ)

Phase

$$-\delta\phi = \phi_{\text{current}} - \phi_{\text{previous}}$$

$$\langle y \cdot \cos(\pi f t) \rangle \simeq \frac{A_e}{2} \sin\phi$$



Overcoming noise / jamming

$$u(t) = p + \text{noise} + A \sin(2\pi f t + \phi)$$

$$\langle u \rangle = p + \langle \text{noise} \rangle + A_e \sin\left(2\pi f \frac{t_i + t_f}{2} + \phi\right) \text{sinc}(\pi f(t_f - t_i))$$

$$\langle \delta^2 u \rangle = \langle \delta^2 \text{noise} \rangle + A^2 \langle \delta^2 \sin \rangle + 2 \underbrace{\langle \delta(\text{noise}) \delta A \rangle}_{\simeq 0}$$



$$2\langle \delta^2 u \rangle_1 - 2\langle \delta^2 u \rangle_2 = A_1^2 - A_2^2 = \delta A^2$$

Parameter - 11

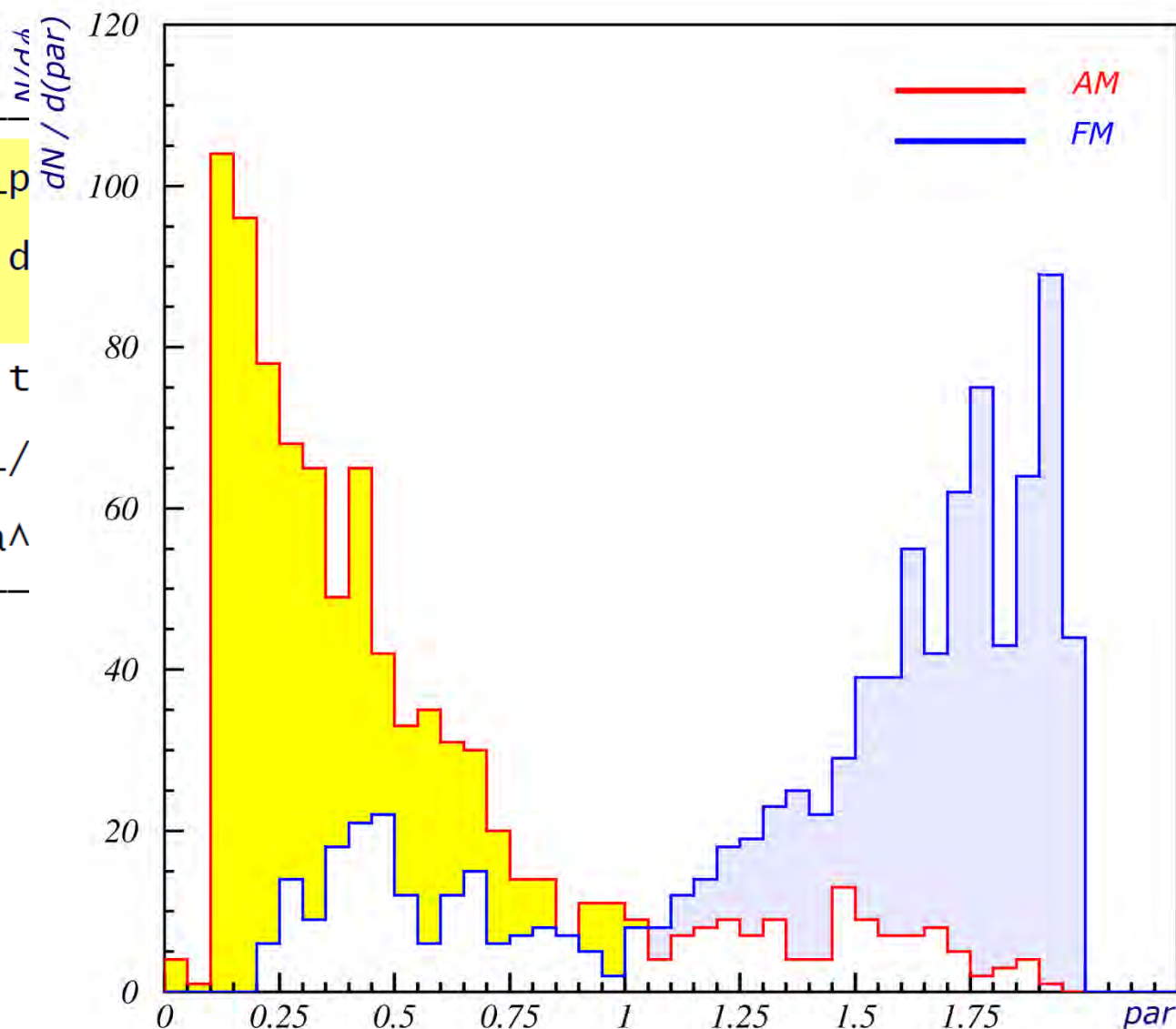
phi 1 = (L2-L1) * d_p

L1 = where d
L2 =

2 = <distr.> in t

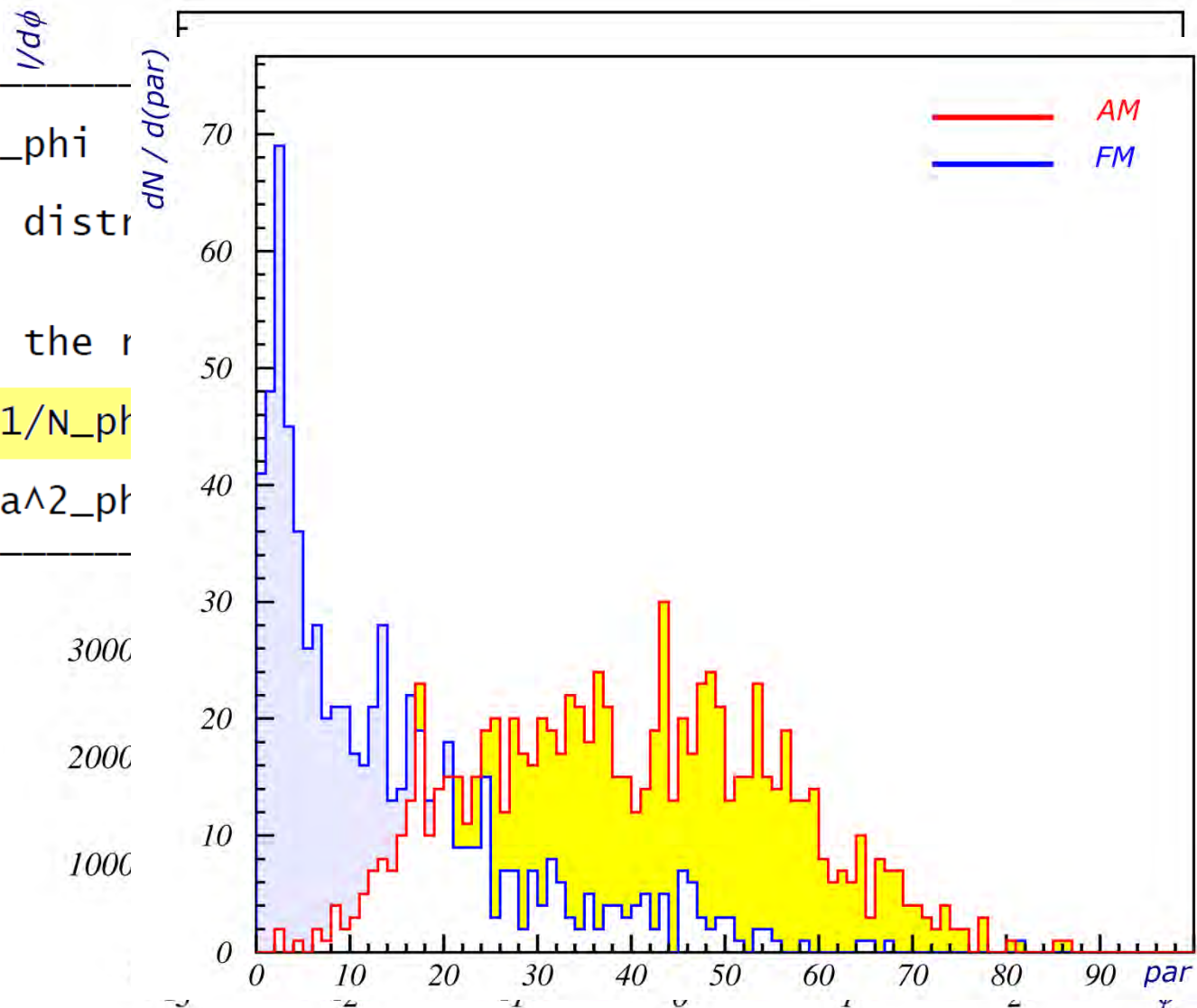
3 = <N_phi> - <1/

4 = <N_phi*delta^



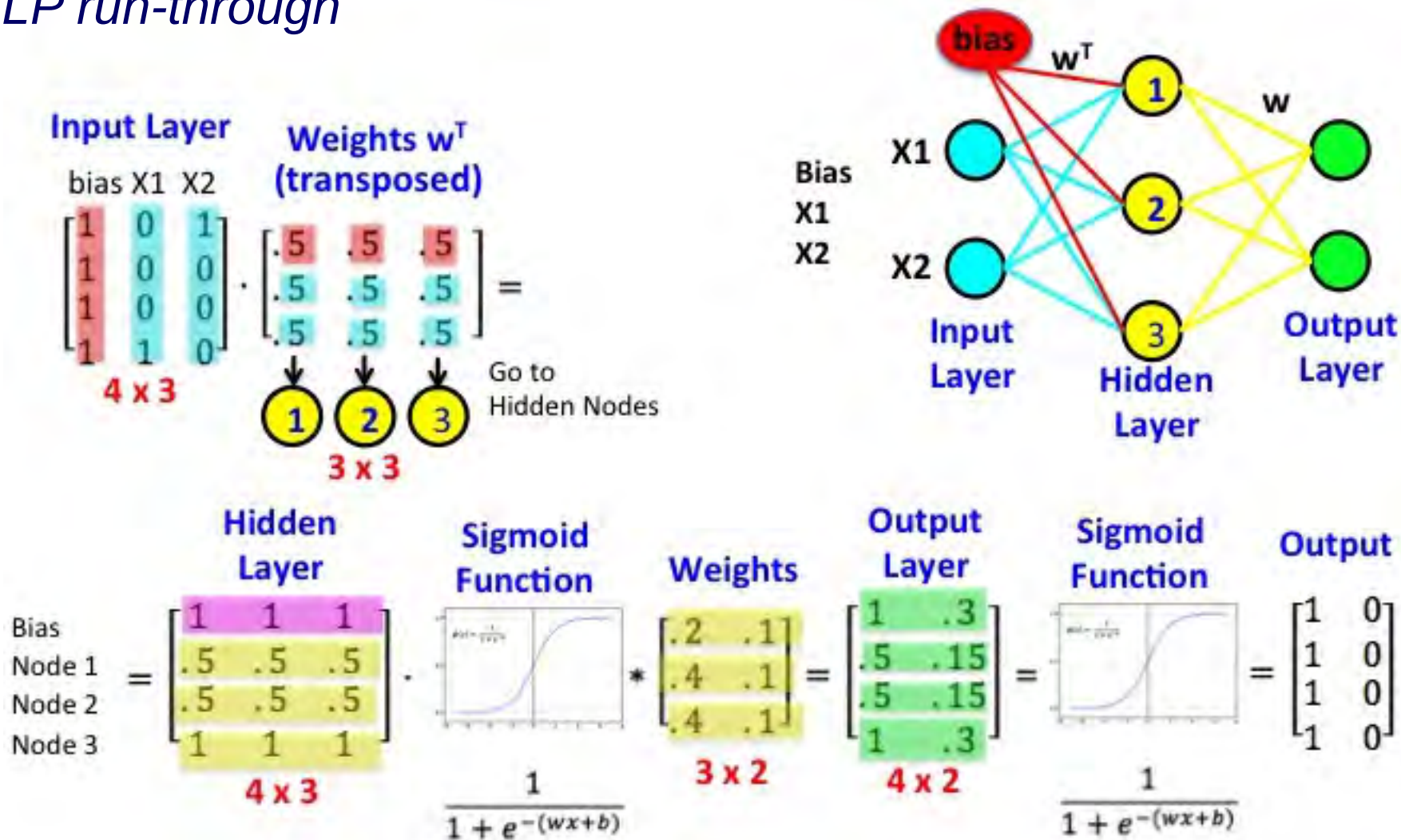
Parameter - 13

$\phi_1 = (L_2 - L_1) * d_{\phi}$
 $L_1 = \text{where distr}$
 $L_2 =$
 $2 = \langle \text{distr.} \rangle \text{ in the } r$
 $3 = \langle N_{\phi} \rangle - \langle 1/N_{\phi} \rangle$
 $4 = \langle N_{\phi} * \delta^2_{\phi} \rangle$



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MLP run-through





ROOT
Reference Guide

Version master ▾

<https://root.cern.ch/doc/master/classTMultiLayerPerceptron.html>

Public Types

enum **EDataset** { kTraining, kTest }

enum **ELearningMethod** {
 kStochastic, kBatch, kSteepestDescent, kRibierePolak,
 kFletcherReeves, kBFGS
}

► Public Types inherited from **TObject**

Public Member Functions

TMultiLayerPerceptron ()

Default constructor. [More...](#)

TMultiLayerPerceptron (const char *layout, const char *weight, **TTree** *data, **TEventList** *training, **TEventList** *test, **TNeuron::ENeuronType** type=**TNeuron::kSigmoid**, const char *extF="", const char *extD="")

The network is described by a simple string: The input/output layers are defined by giving the branch names separated by comas. [More...](#)

Суперкомпьютер
имени Н.Н. Говоруна



ЛАБОРАТОРИЯ
ИНФОРМАЦИОННЫХ
ТЕХНОЛОГИЙ
имени М.Г. Мещерякова

Broyden-Fletcher-Goldfarb-Shanno algorithm - is very popular version of the gradient descent method. It overcomes some of the limitations of plain gradient descent by seeking with the hessian a stationary point of the cost function. The gradient needs to be zero in said point, however neither Newton's method nor BFGS are guaranteed to converge unless the function possesses a quadratic expansion in the vicinity of the optimum.

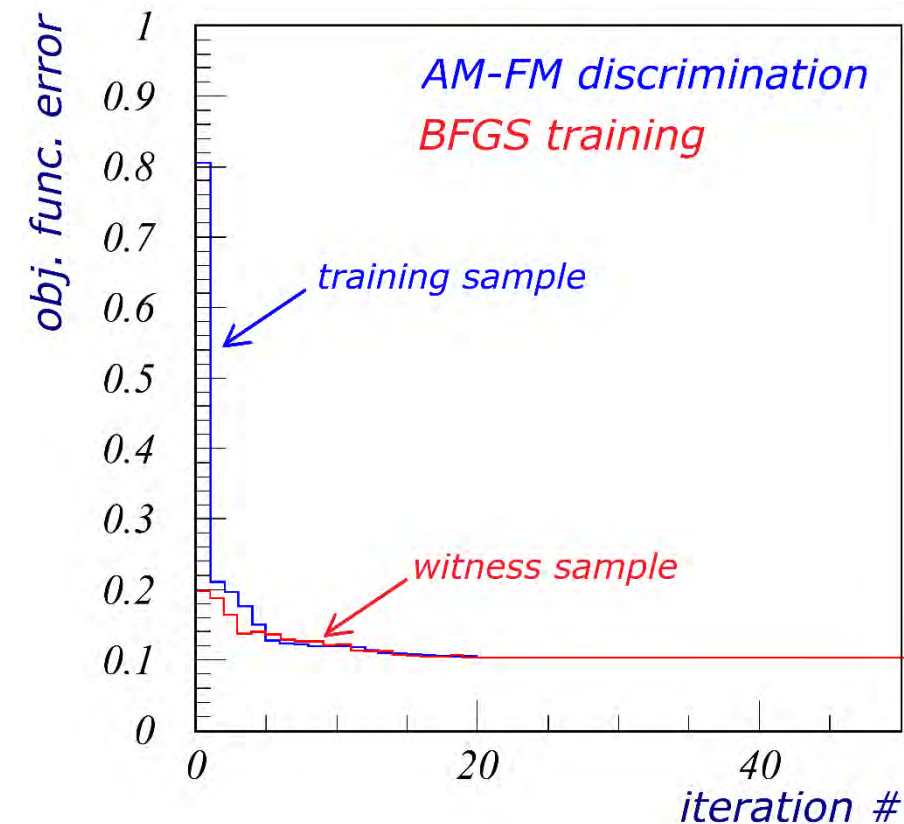
Stochastic Networks

Simulated annealing has been used for many years in the field of numerical optimization. The technique is a special case of the Monte Carlo method.

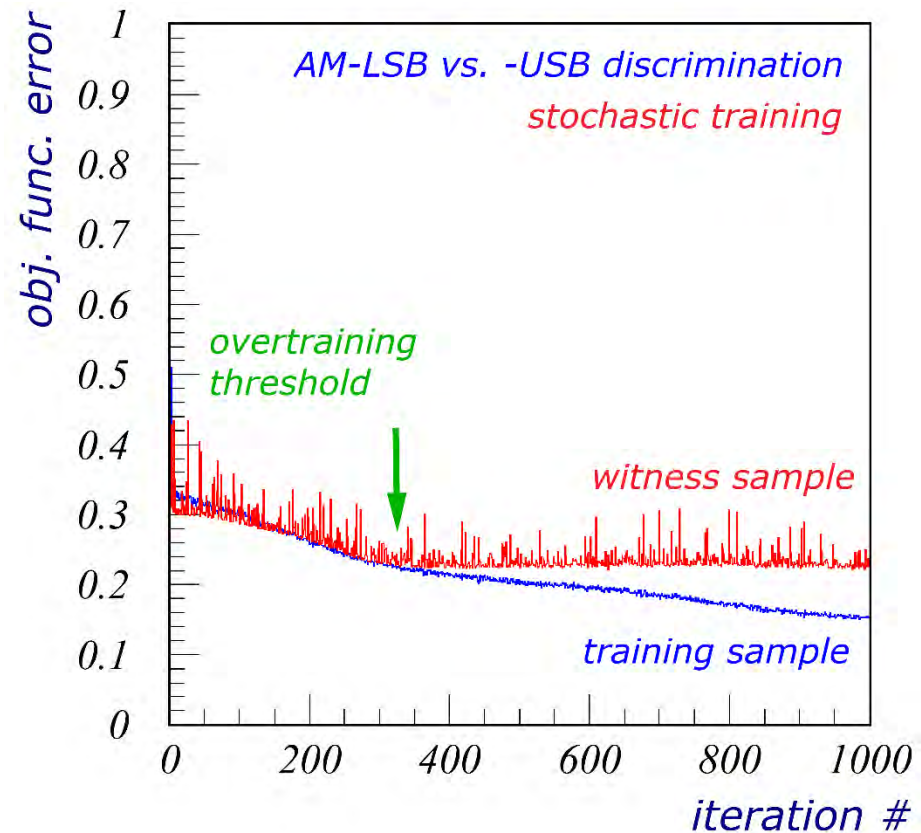
The learning algorithm was the first proposed for stochastic networks and allowed dealing with hidden units in networks of the Hopfield type.

The role of noise in Hopfield networks has been studied by many physicists. It can be shown, for example, that the number of false local minima that arise in Hopfield networks can be compensated with a stochastic dynamic, so that the statistical capacity of the network is improved.

BFGS training

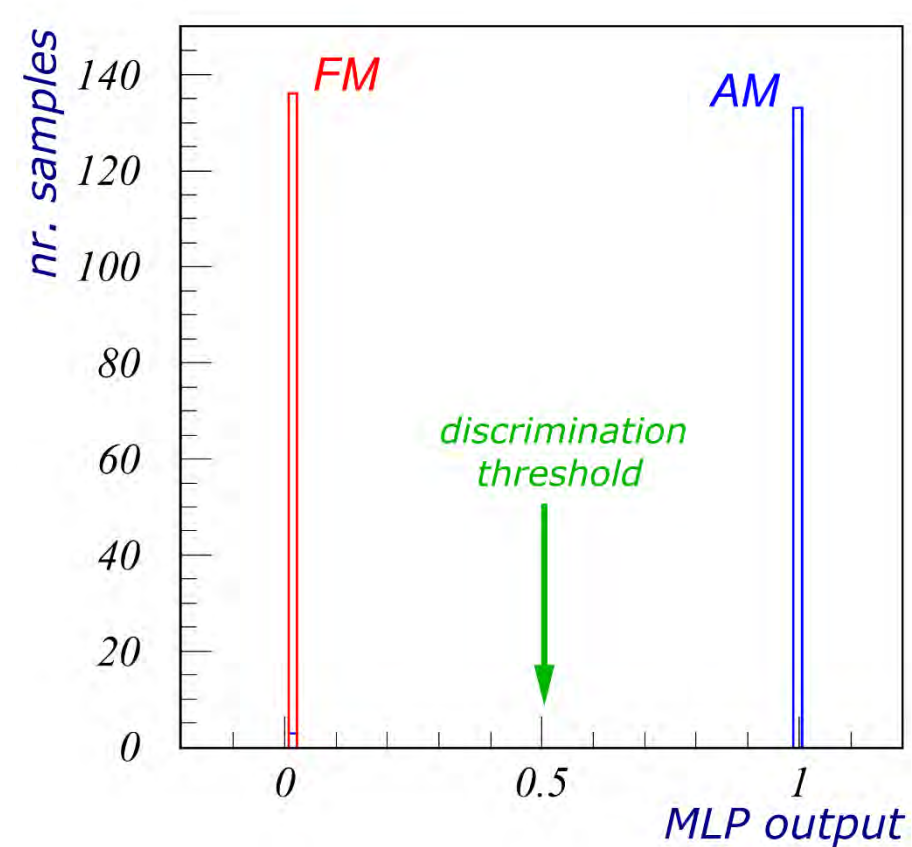


STOCHASTIC training

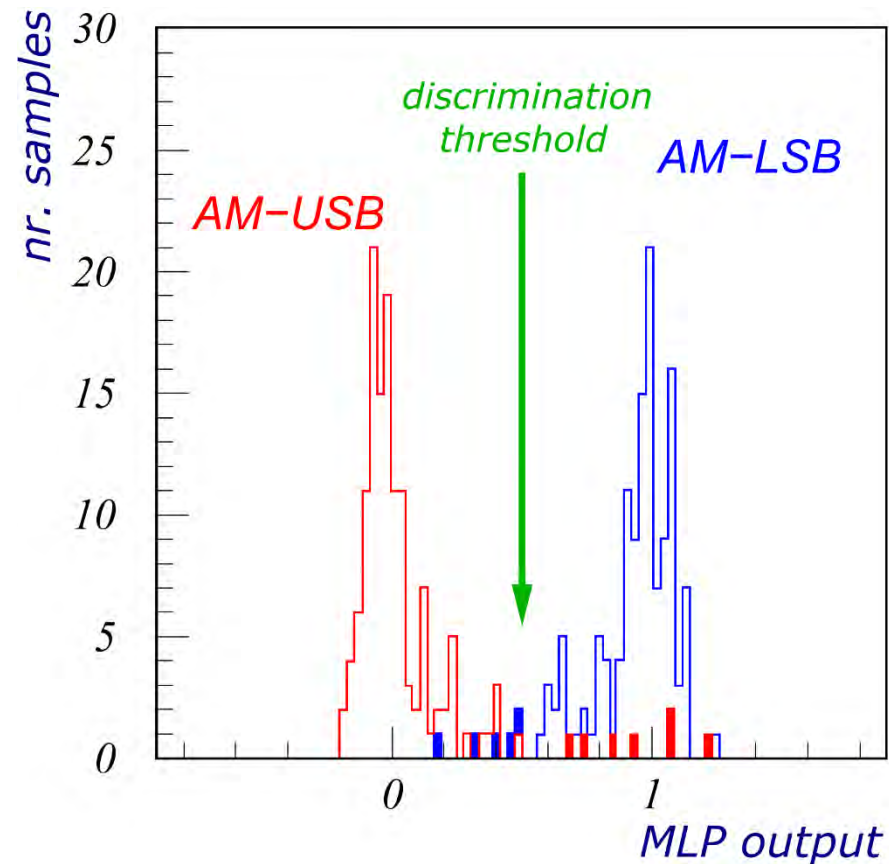


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BFGS training



STOCHASTIC training



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Training method

- BFGS
 - adequate for “strong” distinctive features
 - can get stuck on local-minima
- Stochastic
 - adequate for categories very similar
 - slow, many iterations

Спасибо !